# Optimal Electricity Generation Portfolios in the Presence of Fuel Price and Availability Risks

## Magda Mirescu

University of Vienna and Vienna University of Technology

September 6, 2017





# Why Look Into Electricity Generation?

- Europe-Wide: considerable national and supranational measures for the composition of national electricity generation portfolios (announced or partially implemented already):
  - Nuclear Phase-Out: Italy, Germany, Belgium, Switzerland etc.
  - Subsidies: wind, solar, biomass, combined heat and power plants/systems
  - Targets: 27% renewables by 2030
- Climate Change: ecological motivation or pressure factor
  - o CO2-Emissions: caused by fossil energy
  - Pricing of Emissions: CO<sub>2</sub> European Emission Allowances
- Worldwide: projected growing demand
- ⇒ What is an optimal electricity generation portfolio?

# What is the Setting?

# General (Research) Assumptions

- national decision maker
- economical decision criteria with technical considerations
- several technologies available:
  - thermal and
  - renewable → wind
- each technology type has both advantages and disadvantages
  - o thermal: dispatchable but
    - dirty and dependent on variable input prices
  - o renewable: clean but
    - non-dispatchable and with variable availability

# What is the Research Question?

# Question to Be Answered in This Presentation

What does a cost-optimal electricity generation portfolio consist of, if the decision-maker were to take into account:

- volatility of input prices,
- volatility of (wind) availability and with that coupled higher system costs?

# How to Tackle the Research Question?

# Portfolio Optimization

The process of choosing the proportions of various assets to be held in a portfolio in such a way as to make the portfolio better than any other according to some criterion.

# Distinction Finance - Electricity Economics

- ▶ input: return
- ▶ weights: + und −
- problem:

$$\max_{w} \quad w^{\top} \mu - \frac{\beta}{2} w^{\top} \Sigma w$$
s.t.  $e^{\top} w = 1$ .

- input: LCOE or CF
- ▶ weights: +
- problem:

$$\begin{aligned} & \min_{w} & w^{\top} \mu + \frac{\beta}{2} w^{\top} \Sigma w \\ & \text{s.t.} & e^{\top} w = 1, \\ & w > 0. \end{aligned}$$

# **Data**Overview

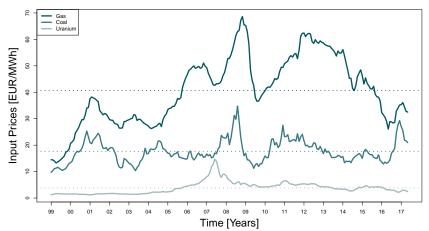
#### ▶ Cost Structure:

IC, FOM, VOM, *Fuel Costs*, Additional System Costs → Germany

- Additional System Costs:
  - Balancing Costs: short-term operational costs a system incurs through output variability and uncertainty.
  - Capacity Costs: costs associated with the required capacity that enables a system to provide system reliability at any time.
- ► Availability Factors: wind speeds → Germany

# Data Input Costs

#### Evolution of the Input Prices in Germany (January 1999 - May 2017)

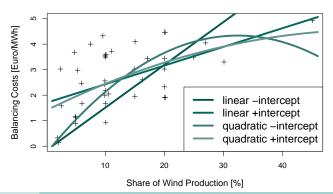


#### **System Costs**

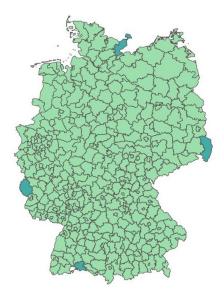
# Balancing Costs Assumptions (Reliability Costs Identical)

▶ linear or quadratic growth in the share of wind generation.

#### Additional Balancing Costs via Wind Integration

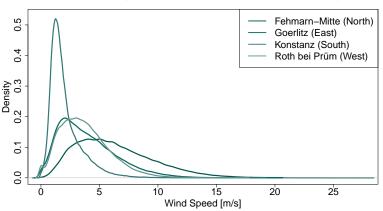


#### Wind Availability - Part 1



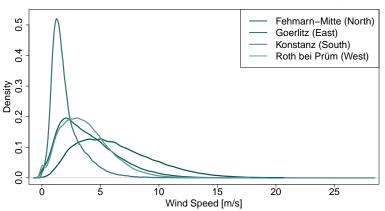
#### Wind Availability - Part 2

#### Kernel Density Estimation at Different Locations in Germany



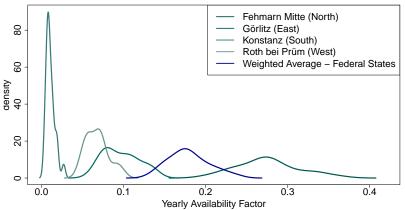
#### Wind Availability - Part 3

#### Kernel Density Estimation at Different Locations in Germany

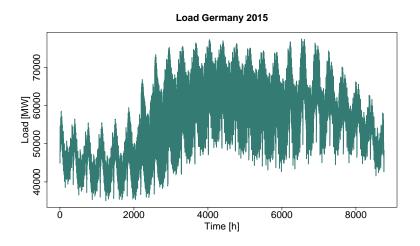


#### Wind Availability - Part 4





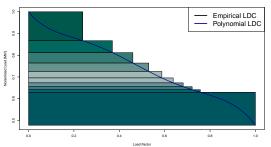
#### Load and Load Duration Curve - Part 1



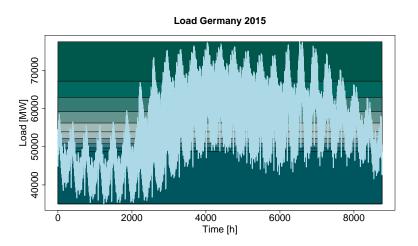
#### Load and Load Duration Curve - Part 2

$$\begin{split} & \min_{\ell_n} & \sum_{n=1}^N (\ell_n - \ell_{n-1}) D(\ell_{n-1}) - \int_{\ell_{n-1}}^{\ell_n} D(l) \mathrm{d}l \\ & \text{s.t.} \int_{\ell_{n-1}}^{\ell_n} D(l) \mathrm{d}l \approx \sum_{n=1}^N (\ell_n - \ell_{n-1}) \frac{D(\ell_{n-1}) + D(\ell_n)}{2} \\ & \ell_0 = 0 \leq \ \ell_n \leq 1 = \ell_N, \end{split}$$

Empirical LDC, Its Polynomial Estimate and Optimally Discretized Blocks - Germany 2015



#### Load and Load Duration Curve - Part 3



# **Mathematical Optimization Model**

$$\min_{x_{i,j}, i \in I, j \in J} \quad \mathbb{E} \big[ \mathbf{c}^{LCOE} \big] + \frac{\beta}{2} \mathbb{V} \mathrm{ar} \big[ \mathbf{c}^{LCOE} \big]$$

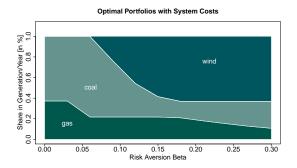
$$\text{s.t.}\underbrace{\left(\begin{array}{cccc} x_{1,1} & \dots & x_{1,J-1} & x_{1,J} \\ \vdots & \ddots & \vdots & \vdots \\ x_{I,1} & \dots & x_{I,J-1} & x_{I,J} \end{array}\right)}_{X} \left(\begin{array}{c} 1 \\ \vdots \\ \mathbb{E}[A(s)] \end{array}\right) = \left(\begin{array}{c} \ell_N D(\ell_{N-1}) \\ \vdots \\ \ell_1(D_{max} - D(\ell_1)) \end{array}\right)$$
 
$$X \geq 0,$$

- ► I... = 3 number of load blocks
  - base, intermediate, peak
- $J \dots = 4$  number of technologies
  - o thermal: coal, gas, nuclear
  - o renewable: wind
- $x_{i,i} \in X$ 
  - electricity generation load block i with technology j
  - decision variable

- consideration of the load via the Load Duration Curve (LDC)
- 2 random variables
  - $\circ$   $A\dots$  availability factor wind
  - $\circ$   $C^{\mathsf{Fuel}}\dots\mathsf{input}\,\mathsf{prices}$
- system costs function f(AXW)
  - none
  - o linear in share of wind generation

## Results

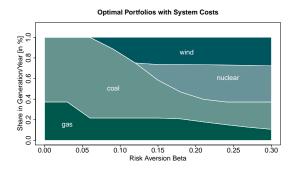
#### Without the Consideration of System Costs



- ► Gas: due to low CF and volatile input costs  $\rightarrow$  peak load for high  $\beta$
- ▶ Coal: lower volatility than gas  $\rightarrow$  replaced by wind for high  $\beta$  (base load)
- Nuclear: too expensive to be a part of the portfolio
- Wind: covers base load only

## Results

#### With the Consideration of System Costs



- Gas: unchanged
- Coal: slightly more
- Nuclear: additional diversification mean → base and intermediate load
- Wind: clearly less → base load only

# **Conclusion**

- A simultaneous consideration of both risk factors appears to be indispensable.
- The diversification effect of wind is
  - overestimated, without considering system costs
  - o smaller, with the consideration of system costs.
- ► The consideration of system costs leads to a non-linear, non-quadratic optimization problem → curse of dimensionality.
  - $\Rightarrow \exists$  trade-off between precision and solvability.

# **Outlook**

- Find a better algorithm to compute the solutions.
- Add several technologies:
  - o hydro,
  - o solar,
  - o lignite.
- Think of a way of modeling the intermittency problem.
- Implement a higher degree system costs function.

# Thank You for Your Attention!

# Dipl.-Ing. Magda Mirescu





#### PhD Student

Vienna University of Technology

Faculty of Mathematics and Geoinformation

Research Group Operations Research and Control Systems (ORCOS)

Wiedner Hauptstraße 8, 1040 Wien

#### Research and Teaching Assistent

**University of Vienna** 

Faculty of Business, Economics and Statistics

Chair of Industry, Energy und Environment (IEE)

Oskar-Morgenstern-Platz 1, 1090 Wien

magda.mirescu@univie.ac.at